



# The simulation of the Electron Tracking Compton Camera with a gaseous time projection chamber and a scintillator

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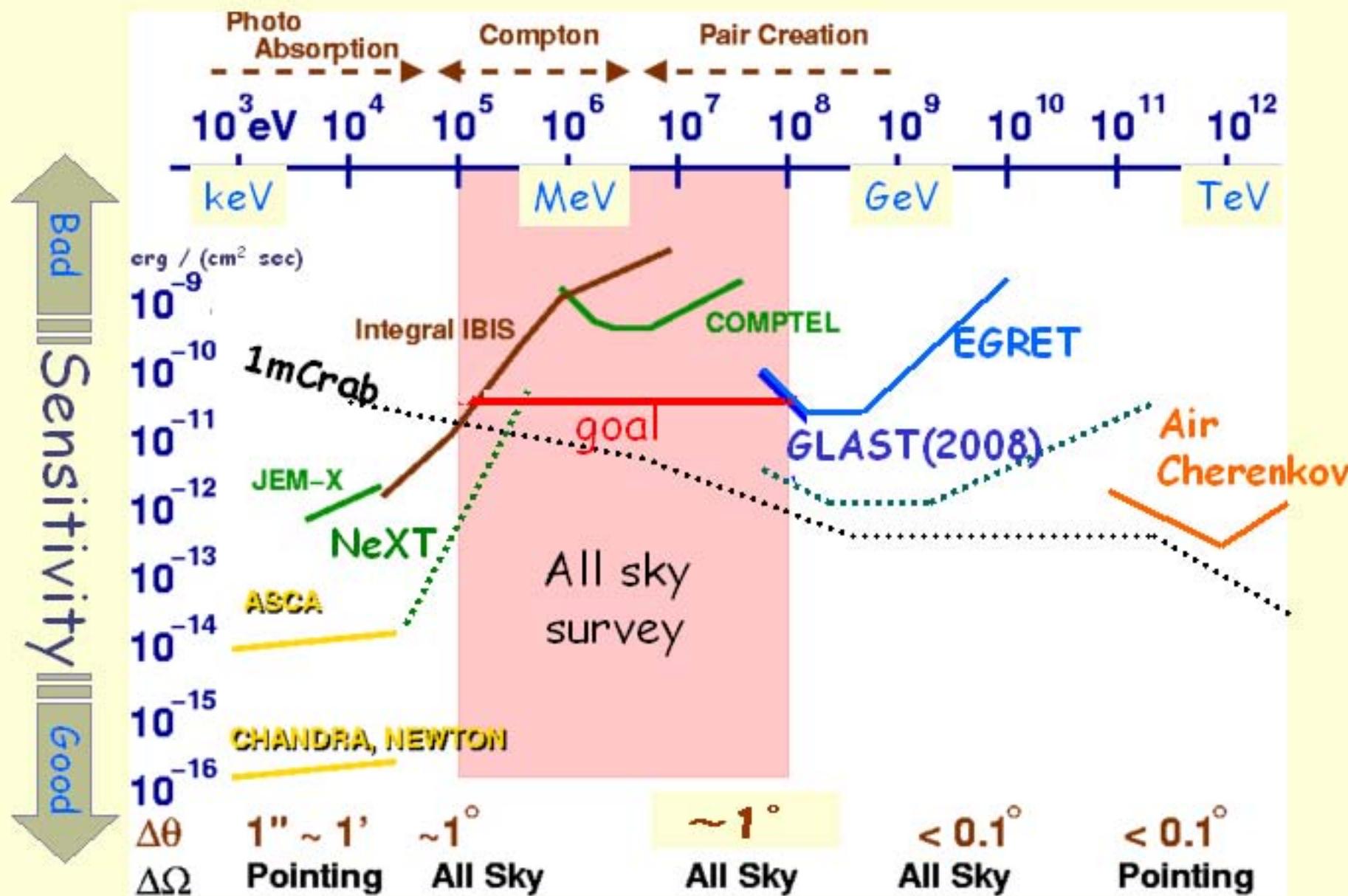
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<sup>3</sup>Kobe Univ., <sup>4</sup>Waseda Univ.

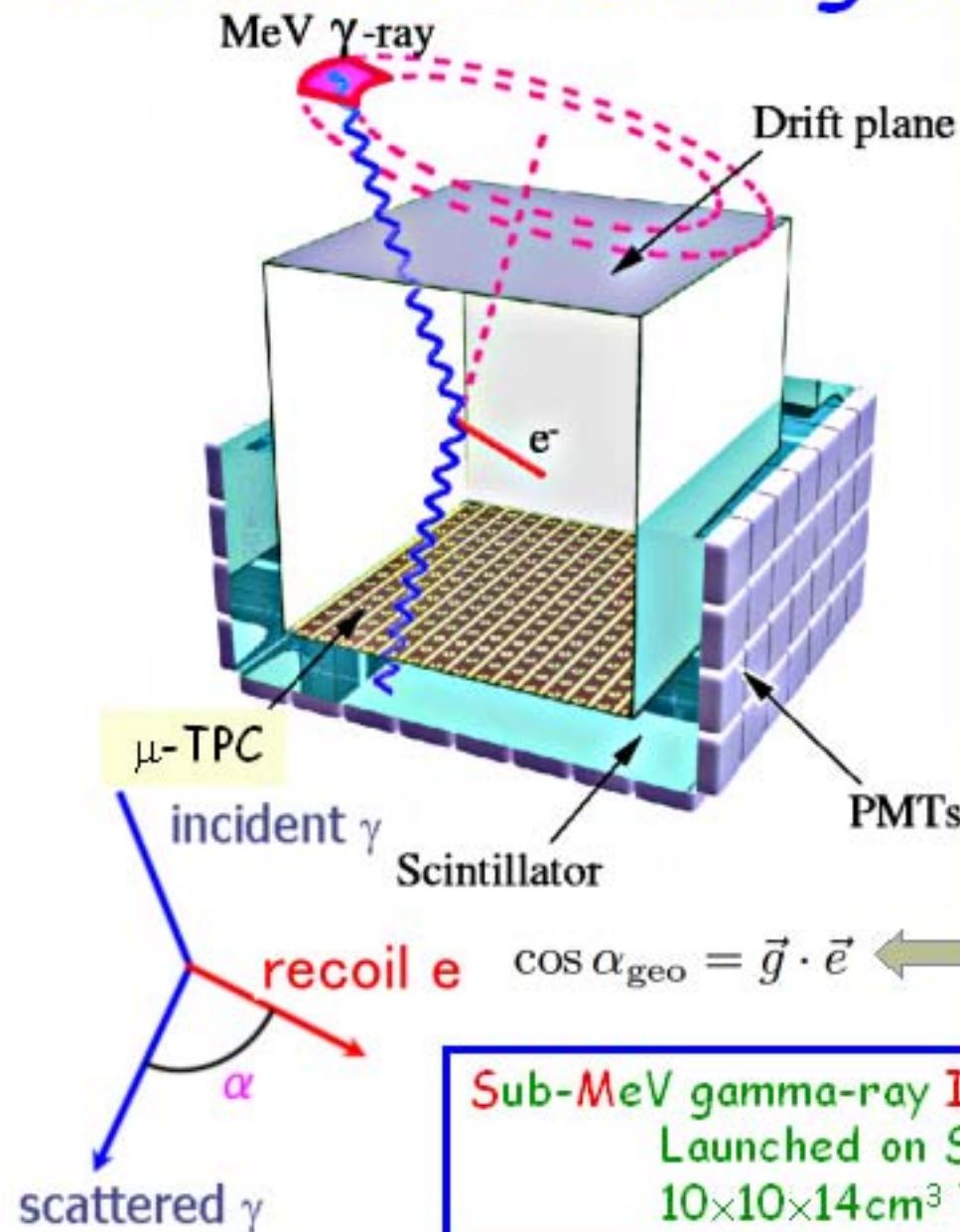
- Introduction
- GSO Pixel Scinti. Camera  
& Time Projection Chamber
- Compton Camera
- Summary



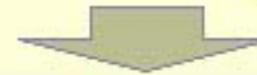
# Sensitivity of X/Gamma-ray observations



# Electron-Tracking Compton Imaging



- ◆ **gaseous TPC : Tracker**  
track and energy  
of recoil electron
- ◆ **Scintillator : Absorber**  
position and energy  
of scattered gamma



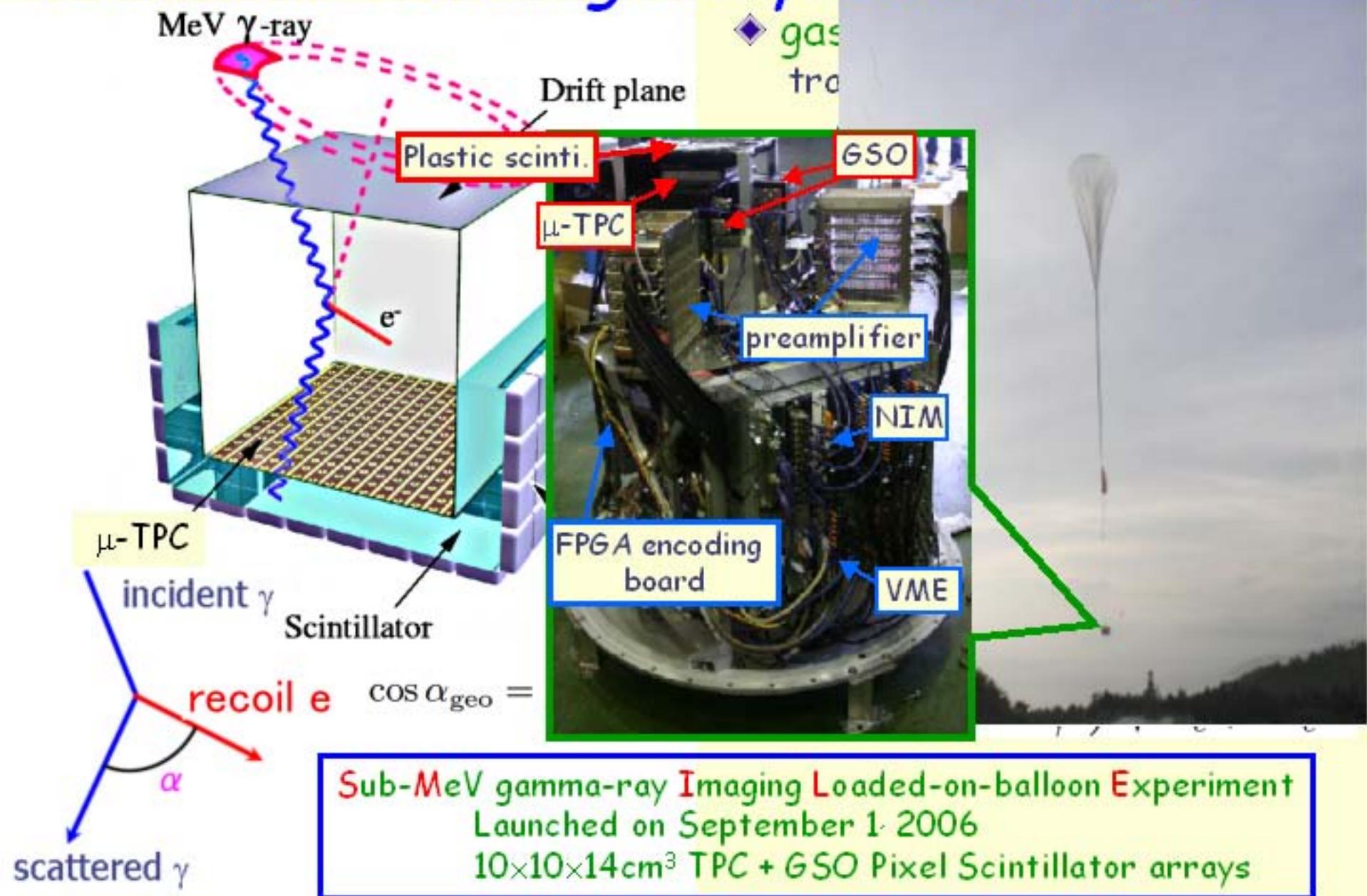
**Reconstruct Compton scattering event by event**

- 1 photon  $\Rightarrow$  direction + energy
- Large FOV ( $\sim 3\text{str}$ )
- Kinematical background rejection

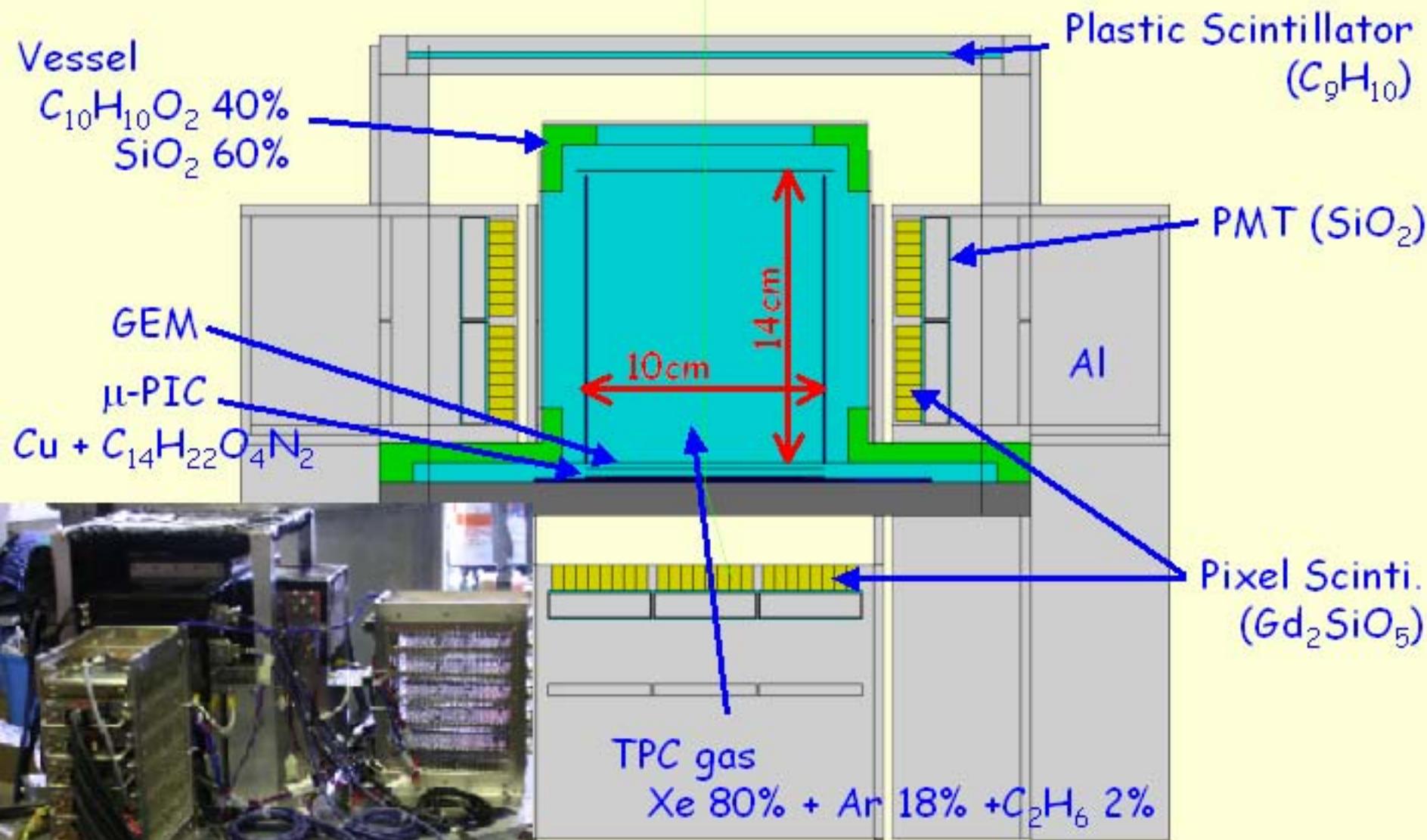
$$\cos \alpha_{\text{geo}} = \vec{g} \cdot \vec{e} \iff \cos \alpha_{\text{kin}} = \left(1 - \frac{m_e c^2}{E_\gamma}\right) \sqrt{\frac{K_e}{K_e + 2m_e c^2}}$$

**Sub-MeV gamma-ray Imaging Loaded-on-balloon Experiment**  
Launched on September 1 2006  
10×10×14cm<sup>3</sup> TPC + GSO Pixel Scintillator arrays

# Electron-Tracking Compton Imaging



# SMILE-I Geometry



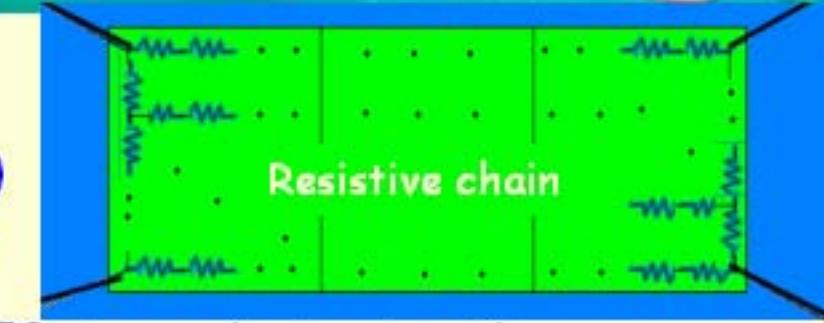
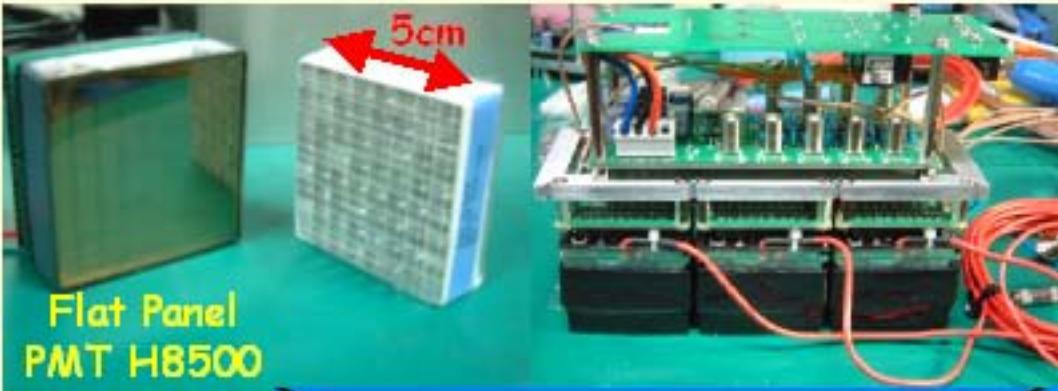
# *Physics List for SMILE-I*

- Gant4.9.0\_p01
- Gamma-ray detection  $\Rightarrow$  Electromagnetic Processes
- Background simulation  $\Rightarrow$  Hadronic Processes
- Based on the physics list of  
'examples/advanced/underground\_physics'
- The several alterations
  - Compton/Rayleigh scattering for gamma  
 $\Rightarrow$  **LECSCompton/Rayleigh**  
For the Doppler broadening  
(<http://public.lanl.gov/mkippen/actsim/g4lecs>)
  - For the charged particles  
 $\Rightarrow$  **G4StepLimiter** in TPC  
Tracing the tracks with the pitch of **less than 40  $\mu\text{m}$**

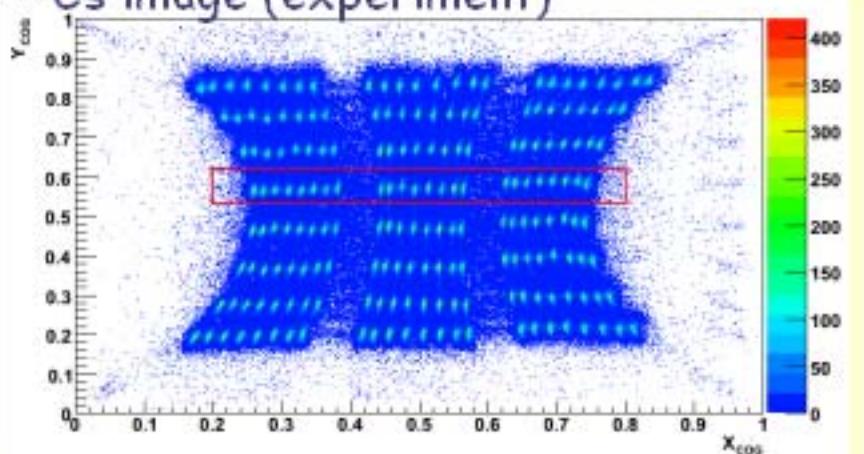
# GSO Pixel Scintillator Array

# Simulation of Absorber

- Scintillator : GSO(Ce)
- Pixel size :  $6 \times 6 \times 13 \text{ mm}^3$
- $8 \times 8$  pixels  $\Rightarrow$  1 array
- 3 PMTs  $\Rightarrow$  1 unit
- Photo readout : H8500 (HPK)  
gain uniformity is not good  
(Min:Max = 1:2~4)  
light cross-talk at window  
(~40% leaks to surrounding pixels)
- 4 channels readout with resistive chain  
incomplete quantization  
distorted image
- Energy resolution :  
Average 10.9% (662keV, FWHM)  
inside (6x6 pixels) : 10.5%  
outside (28 pixels) : 11.5%



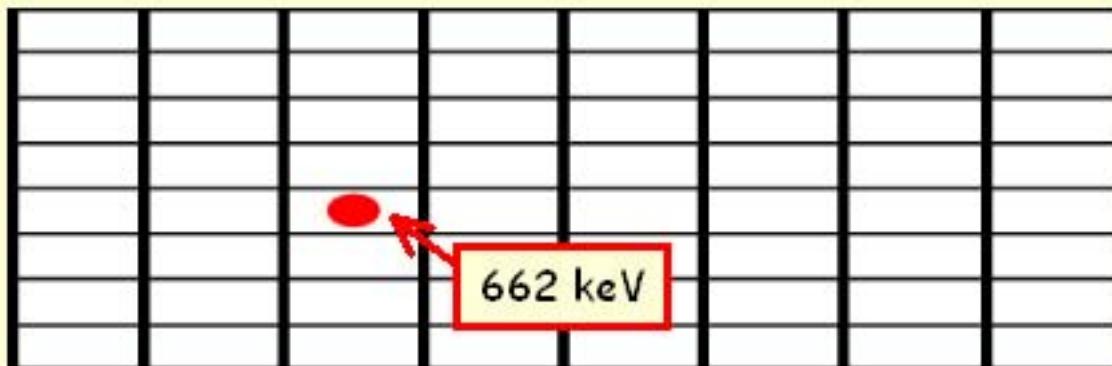
$^{137}\text{Cs}$  image (experiment)



# Simulation of Absorber

1. Geant4  $\Rightarrow$  pixel ID, deposit energy  $E$
2. Obtain the light cross-talk rate  $l_i$  of each pixel.

center	1
horizontal	Gauss (mean: 0.153, RMS: 0.0265)
diagonal	Gauss (mean: 0.0323, RMS: 0.00951)
3. Calculate the detected charge of each anode  
considering with **energy resolution**.  
$$\text{Gauss (mean: } El_i, \text{ RMS: } 1.2 \times (El_i)^{0.5} \text{)}$$
4. multiply the **gain map of PMT** by the detected energy.
5. Divide the obtained charge to **4 channel readouts** using a template.
6. Add the **pedestal** to each readout.
7. reconstruct the image by the charges of 4 channel readouts.



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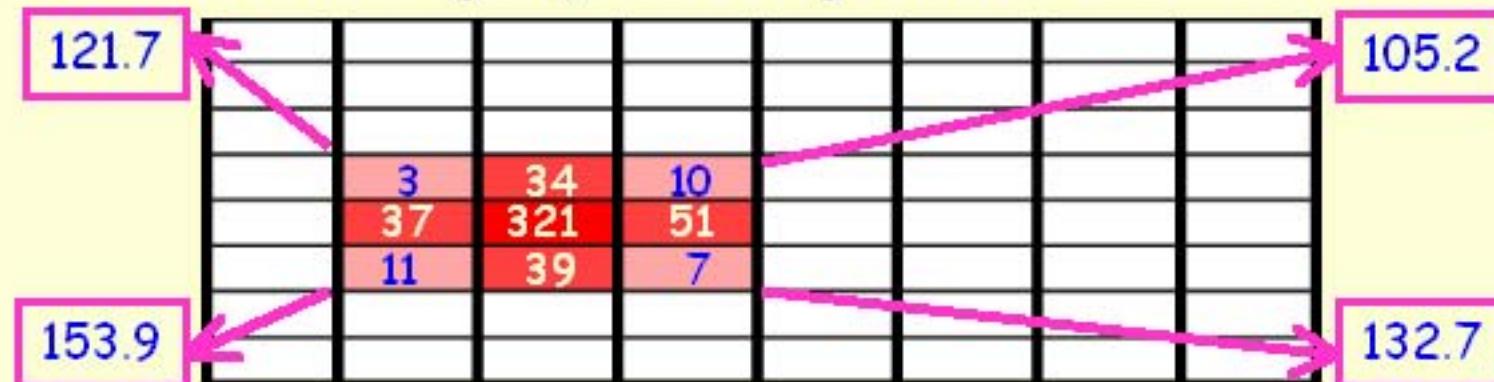
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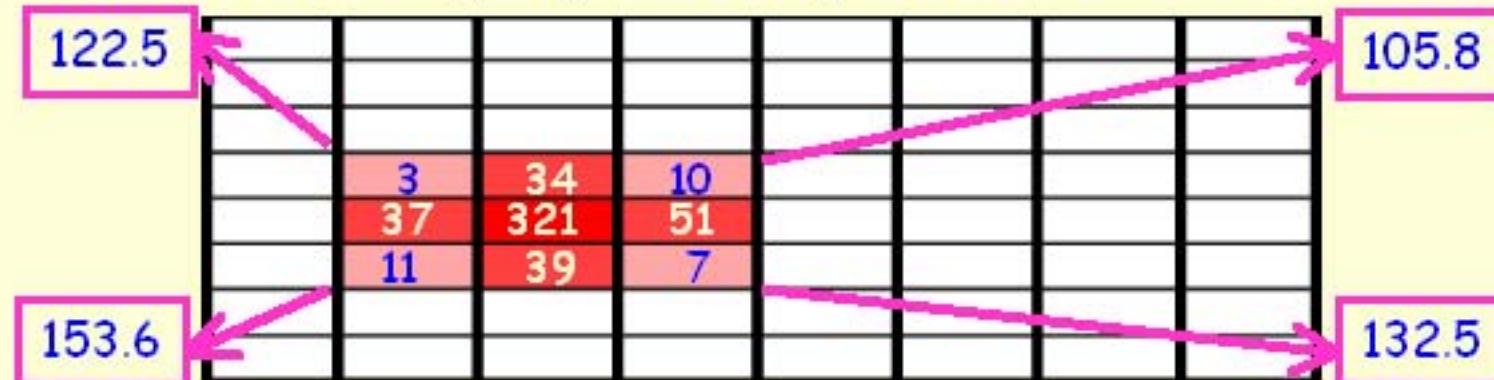
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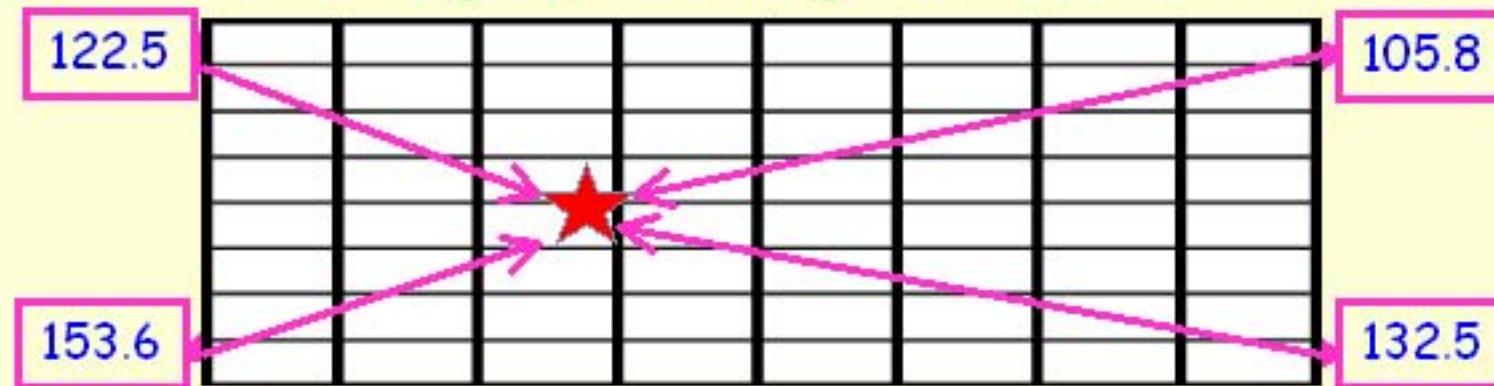
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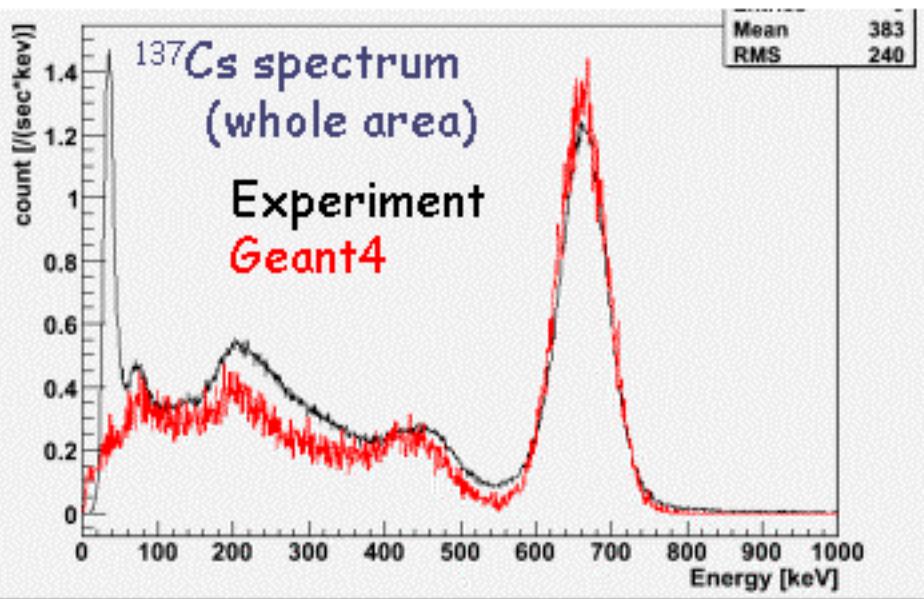
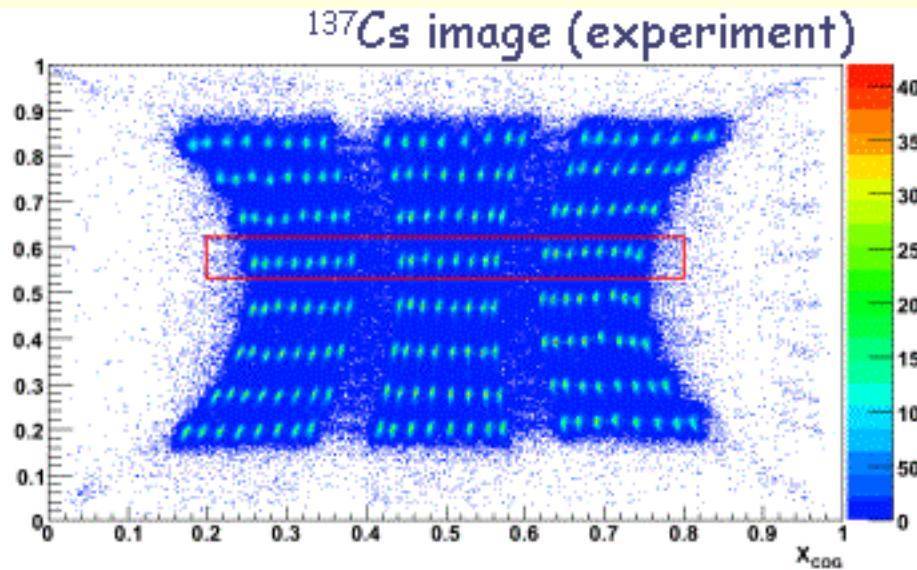
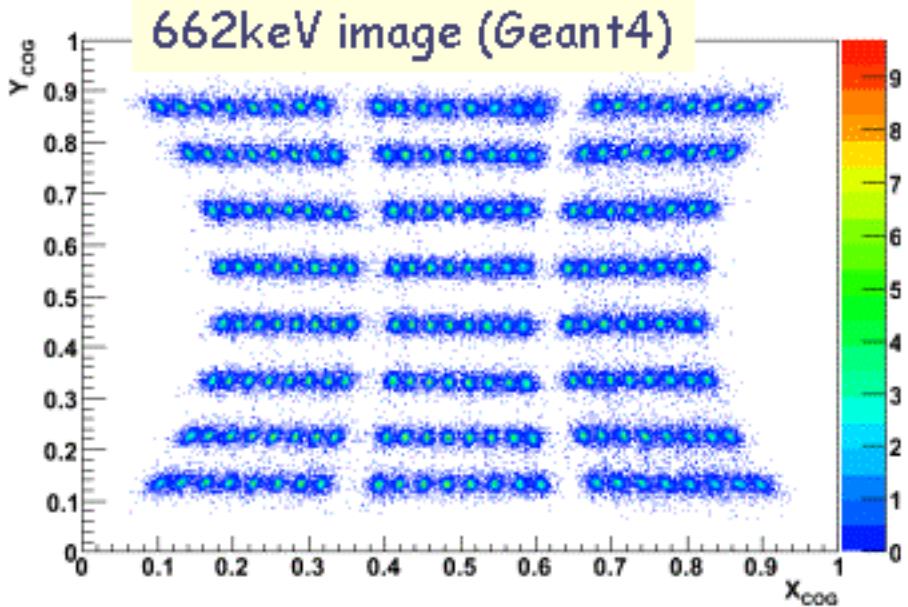
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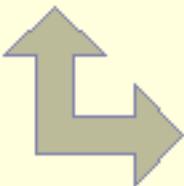


# Simulation of Absorber



Energy resolution  
Geant4

Whole : 11.3%  
inside : 10.5%  
outside : 12.3%



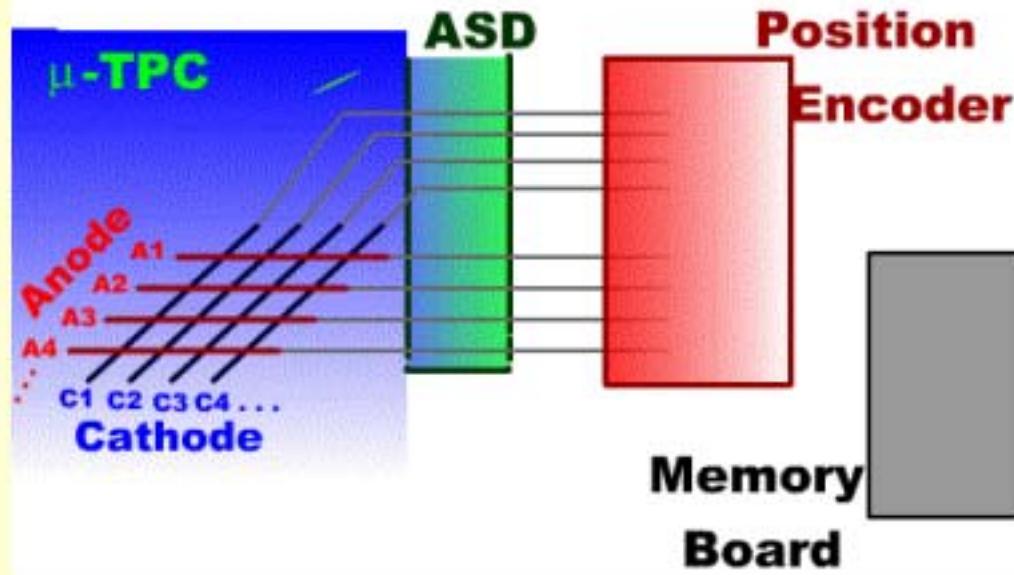
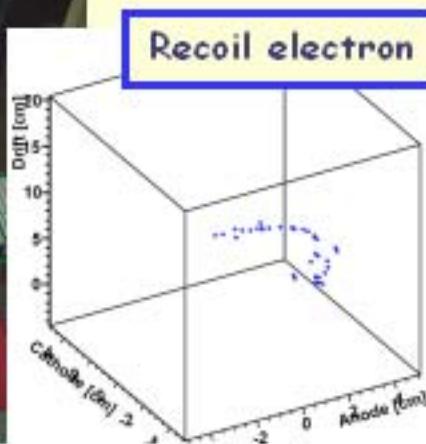
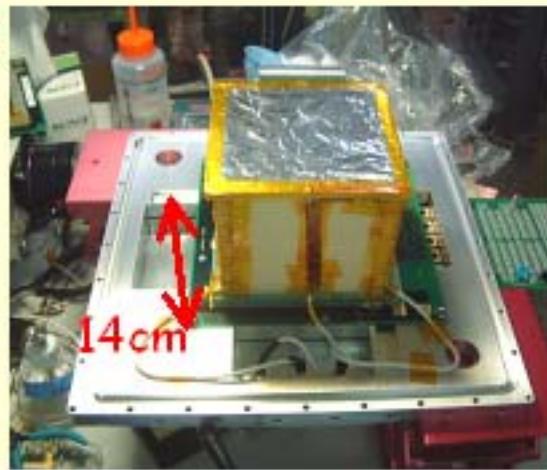
Experiment

Whole : 10.9%  
inside : 10.5%  
outside : 11.5%

# Electron Tracker

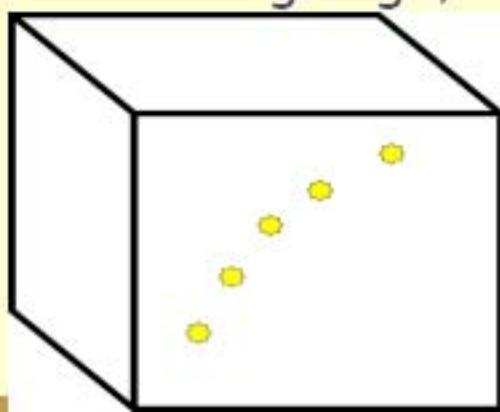
# Simulation of Tracker

- Gas : Xe 80% + Ar 18% +  $C_2H_6$  2%  
1atm, sealed,  $10 \times 10 \times 14$  cm $^3$
- w value : 23 eV
- Diffusion : (Magboltz simulation)  
transverse 0.52mm/ $\sqrt{\text{cm}}$   
longitudinal 0.28mm/ $\sqrt{\text{cm}}$
- Strip readout (**0.40mm pitch**)
- Gas Gain :  $\sim 30000$
- Preamp :  $\tau = 16$  nsec,  $C = 1\text{pF}$
- Drift velocity ( $V_d = 400\text{V/cm}$ ) :  
measured **2.4 cm/ $\mu\text{sec}$**
- calculate the track points  
with **100 MHz**
- Energy resolution :  
 **$\sim 45\%$**  (22.2keV, FWHM)
- Position resolution :  **$\sim 0.5\text{mm}$**



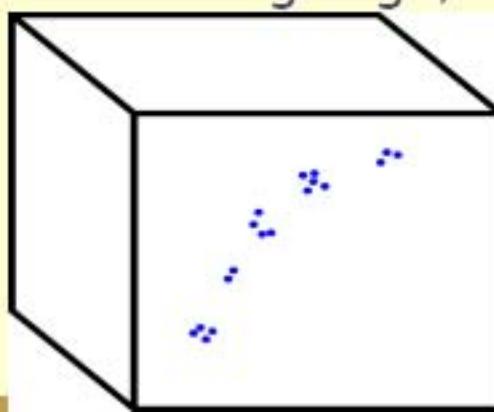
# Simulation of Tracker

1. Geant4  $\Rightarrow$  position  $\mathbf{x}$ , deposit Energy  $E$  (pitch  $< 40 \mu\text{m}$ )
2. Obtain the number  $n$  of ionized electron at  $\mathbf{x}$ .  
Poisson (mean:  $E/w$ )
3. Calculate the diffusion which is the function of the drift length  $d$ .  
transverse      Gauss (RMS:  $0.52\sqrt{d} \text{ mm}$ )  
longitudinal      Gauss (RMS:  $0.28\sqrt{d} \text{ mm}$ )
4. Quantize to the strip readout and sampling clock.  
 $x/y$       0.4 mm pitch       $\Leftarrow$  readout pitch of  $400 \mu\text{m}$   
 $z$       0.24 mm pitch  
 $\Leftarrow$  drift velocity  $2.4 \text{ cm}/\mu\text{sec}$ , 100MHz sampling
5. Calculate the detected charge considering with energy resolution.
6. Calculate the wave form using the response template of the preamp.
7. take the leading edge, and take the coincidence between  $x$  and  $y$ .



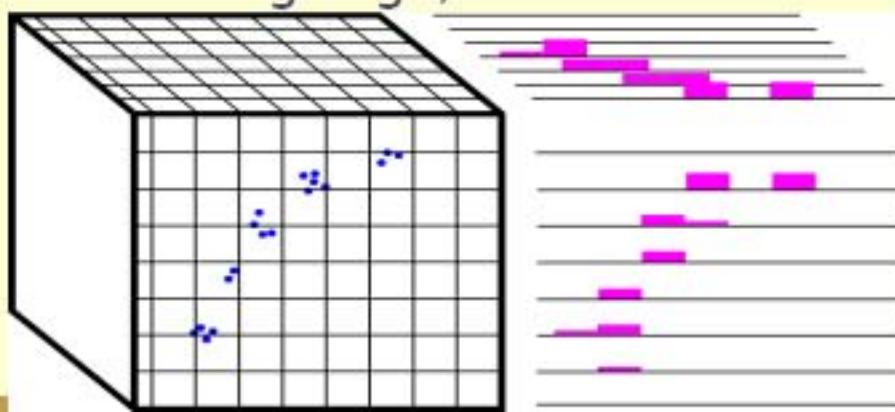
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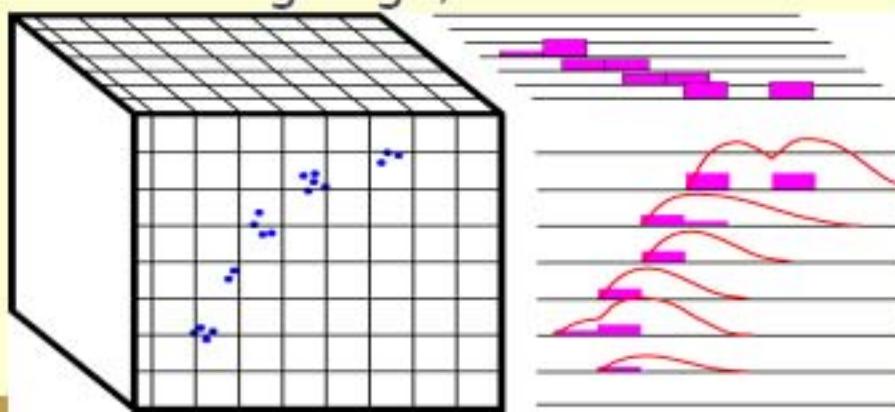
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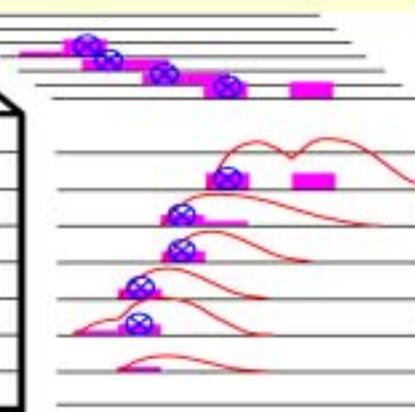
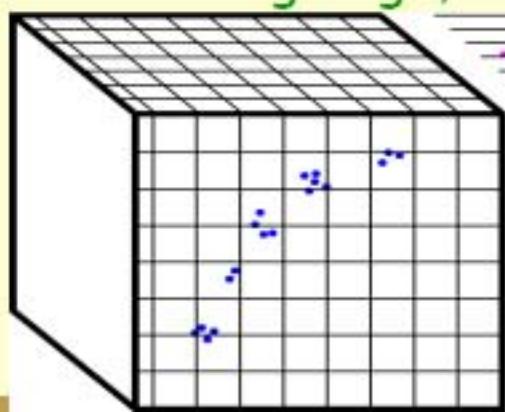
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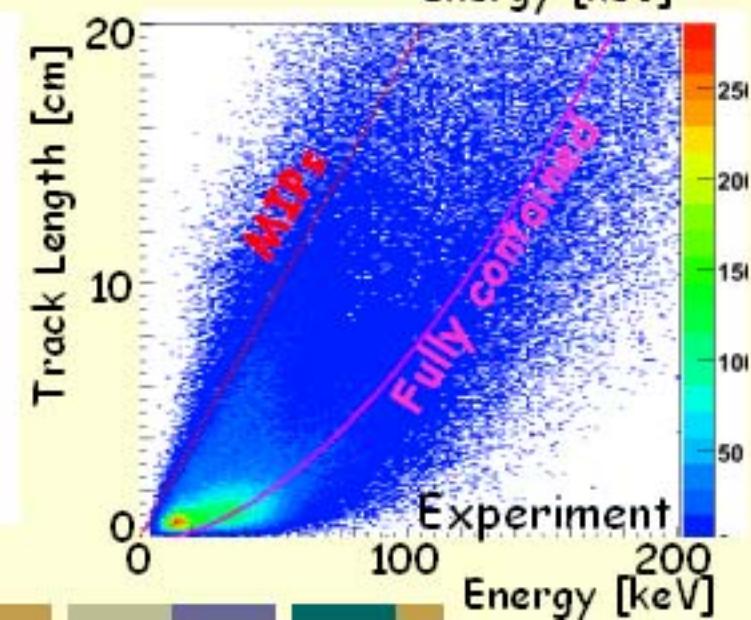
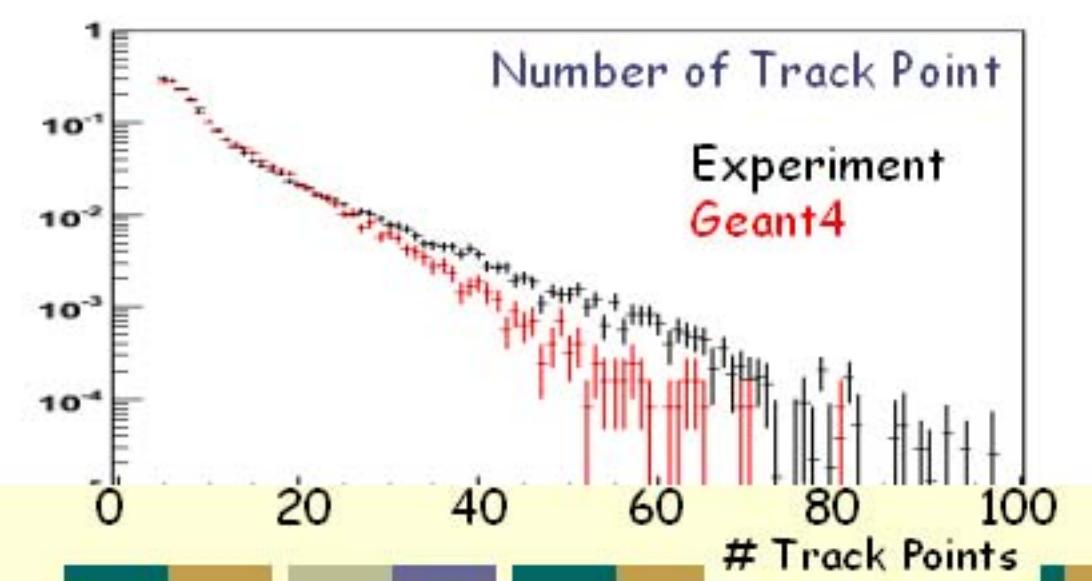
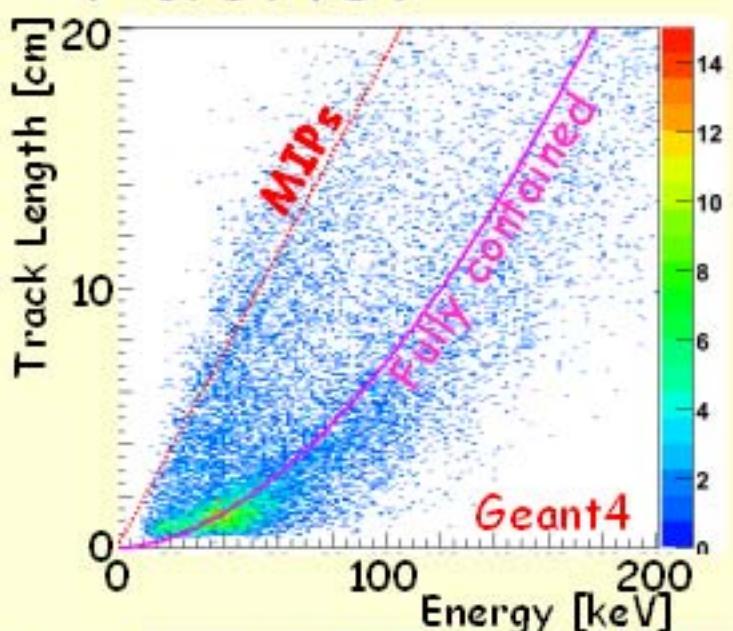
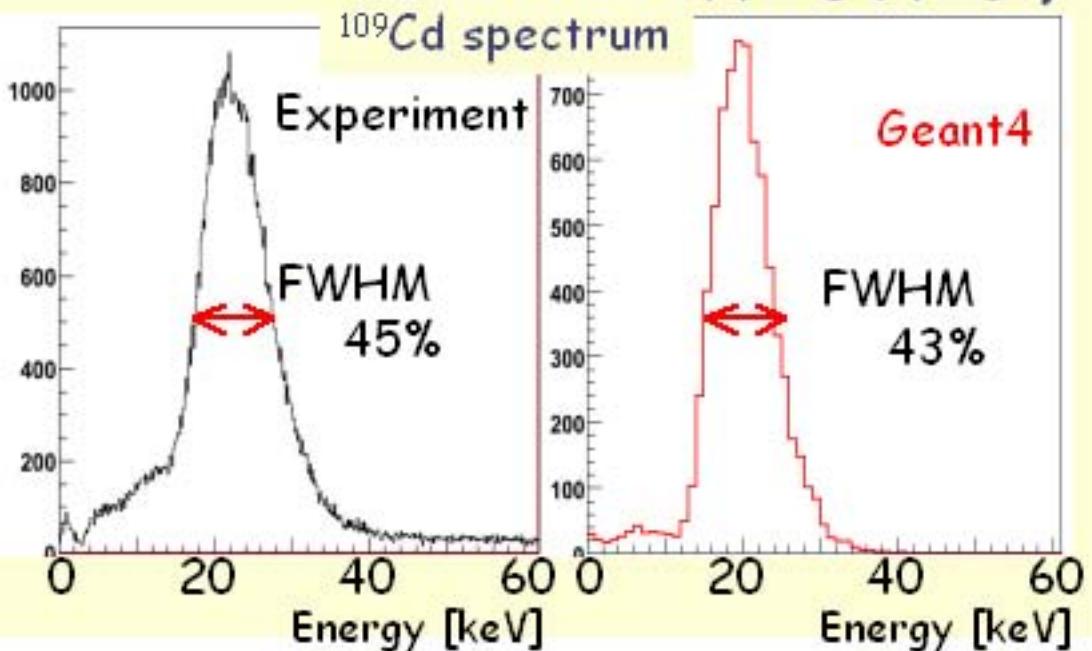
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7. take the leading edge, and take the coincidence between x and y.



	X	Y	Z
	3.5	3.5	2
	5.5	2	3
	7	1	4

# Simulation of Tracker

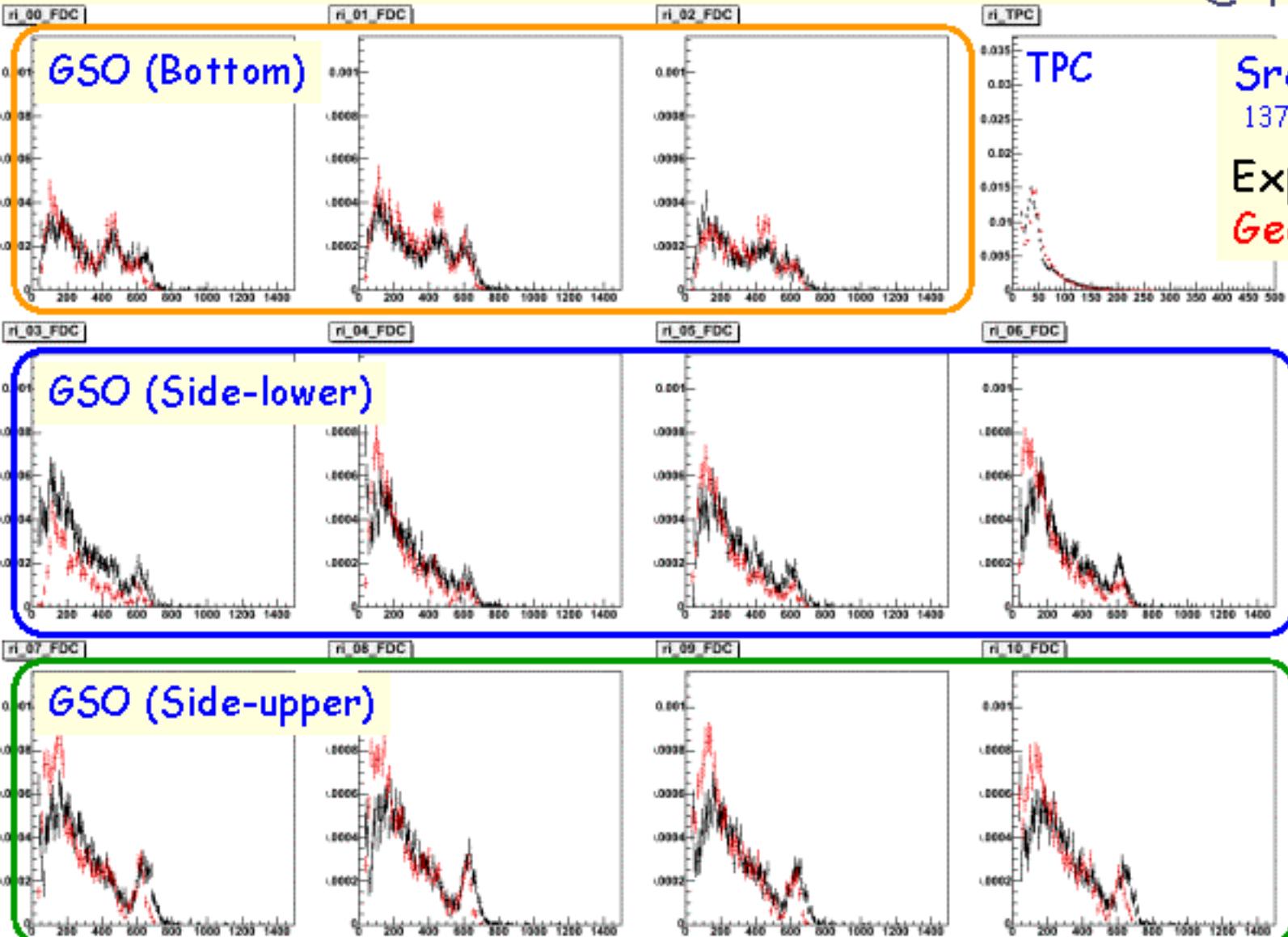




# Electron Tracking Compton Camera (ETCC)

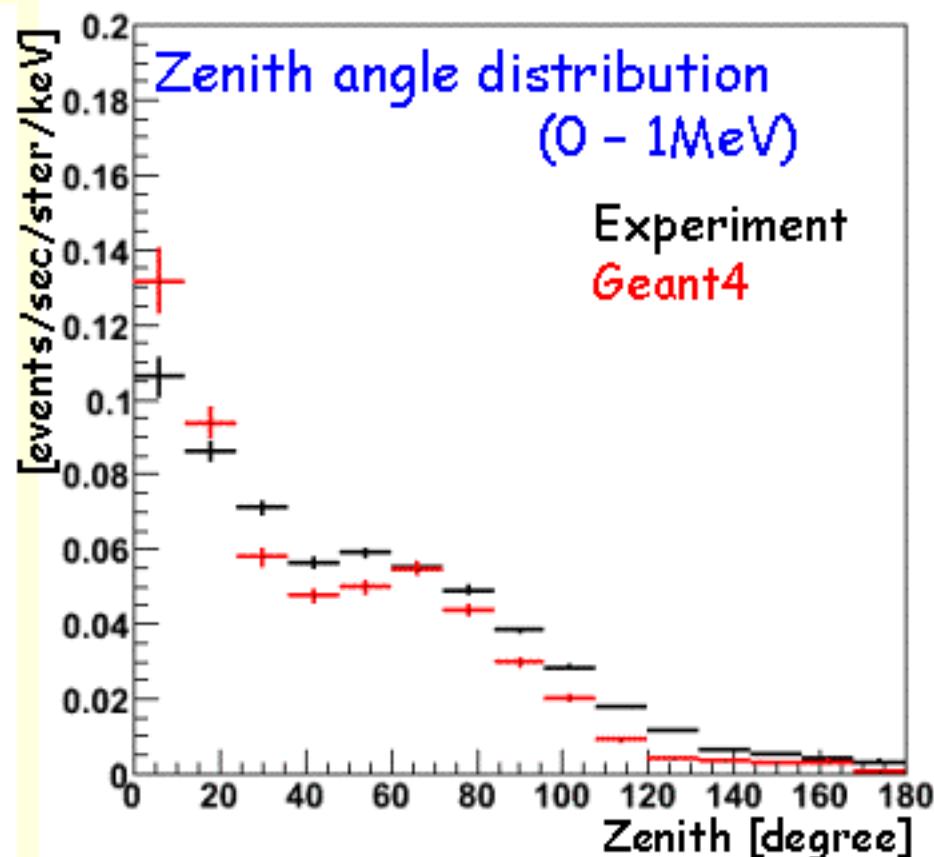
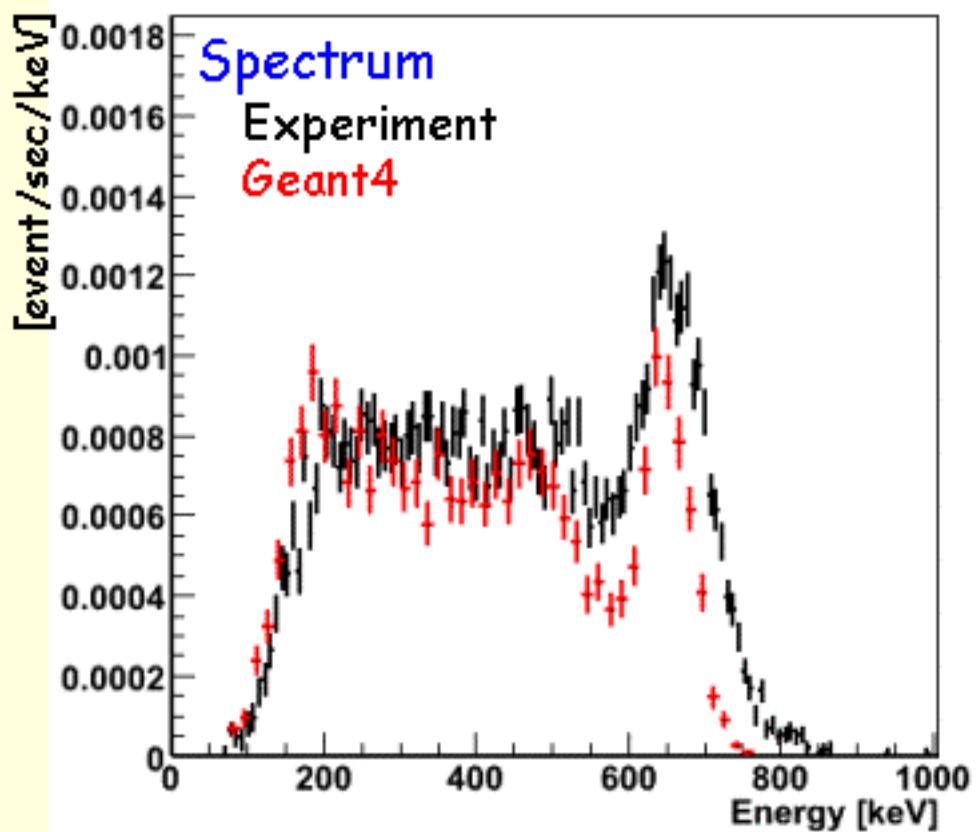
# Spectra of GSO units/TPC

@ fiducial cut



# Reconstruction of gamma-ray

Src:  $^{137}\text{Cs}$  (662keV), on-axis, 55cm from window

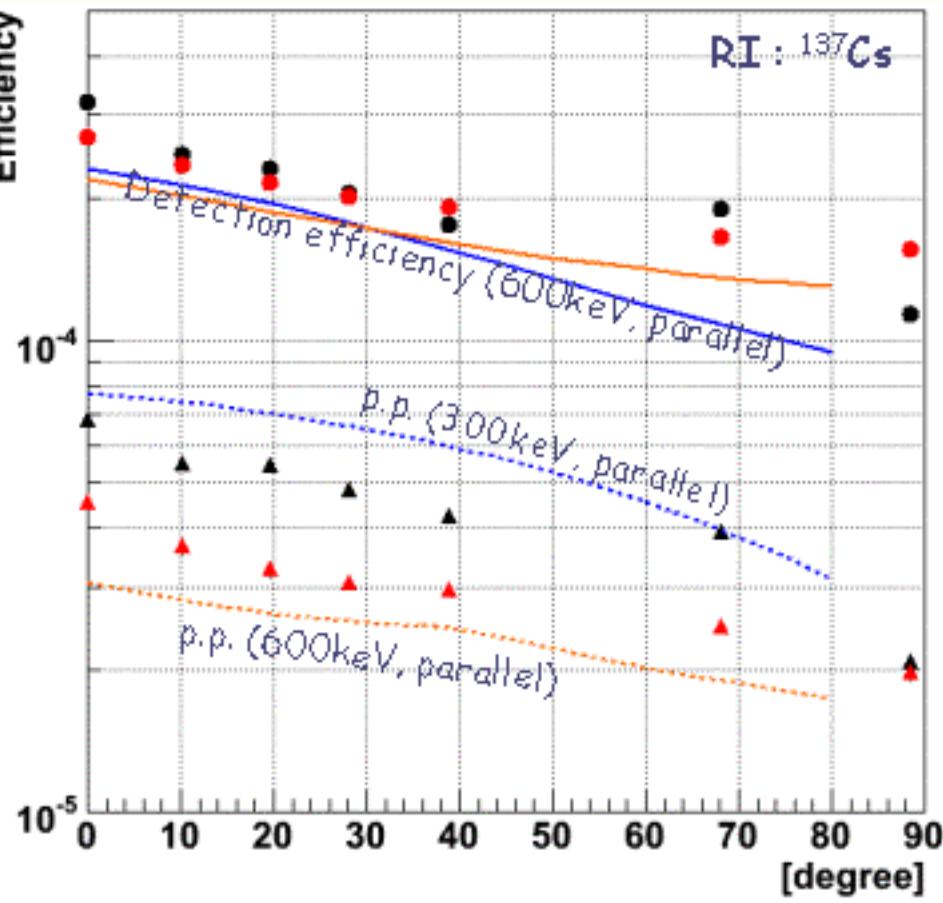
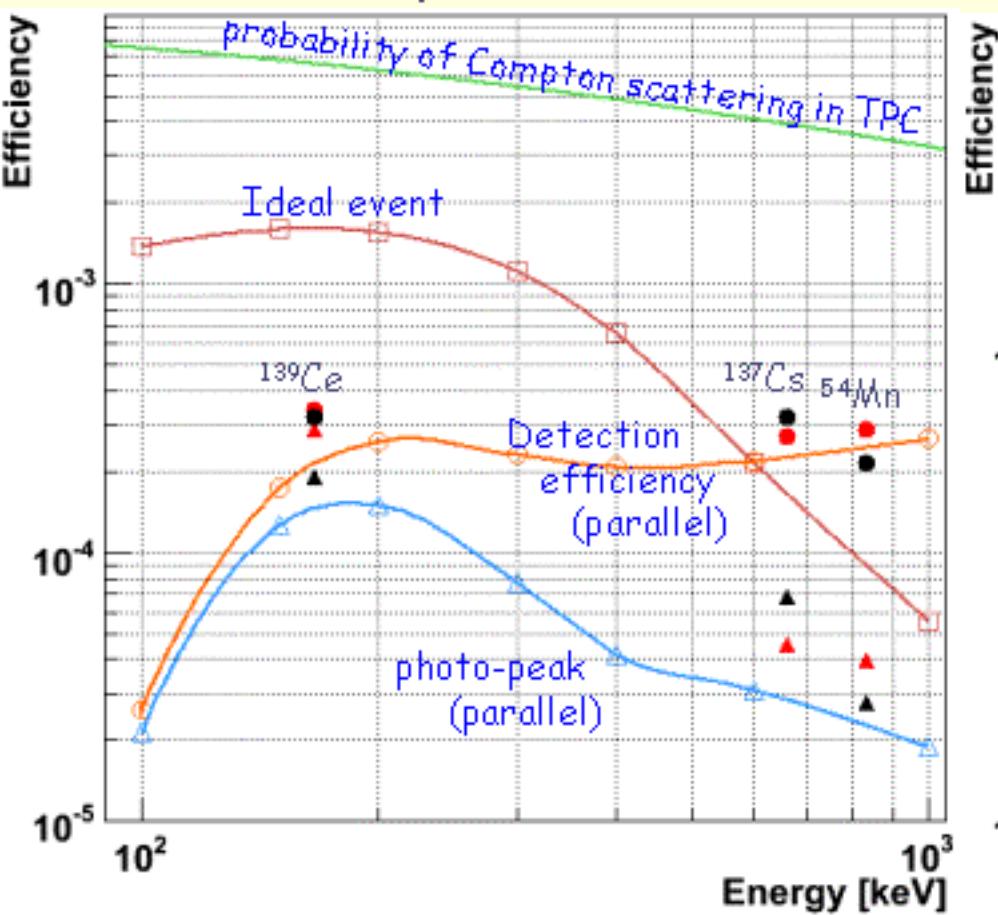


- We succeeded in the reconstruction of gamma-rays by both experiment and simulation.
- The simulation are roughly consistent with the experiment.

# Detection Efficiency & FOV

- : Detection Efficiency for RI source
- ▲: Photo-peak for RI source

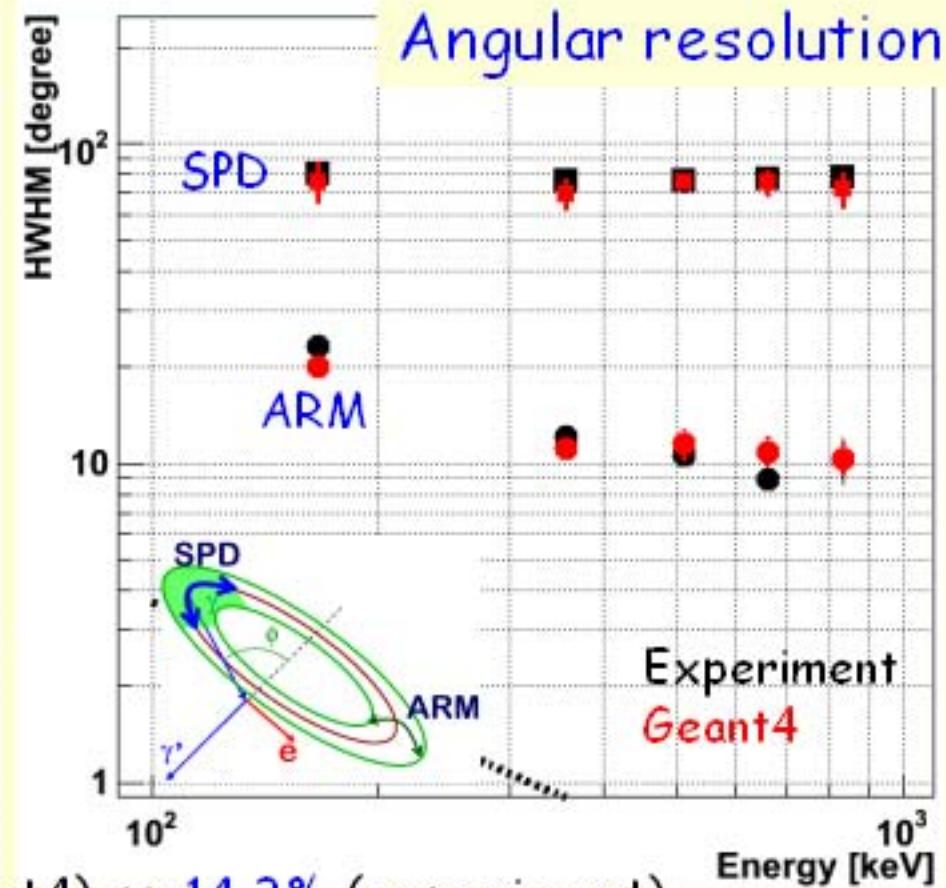
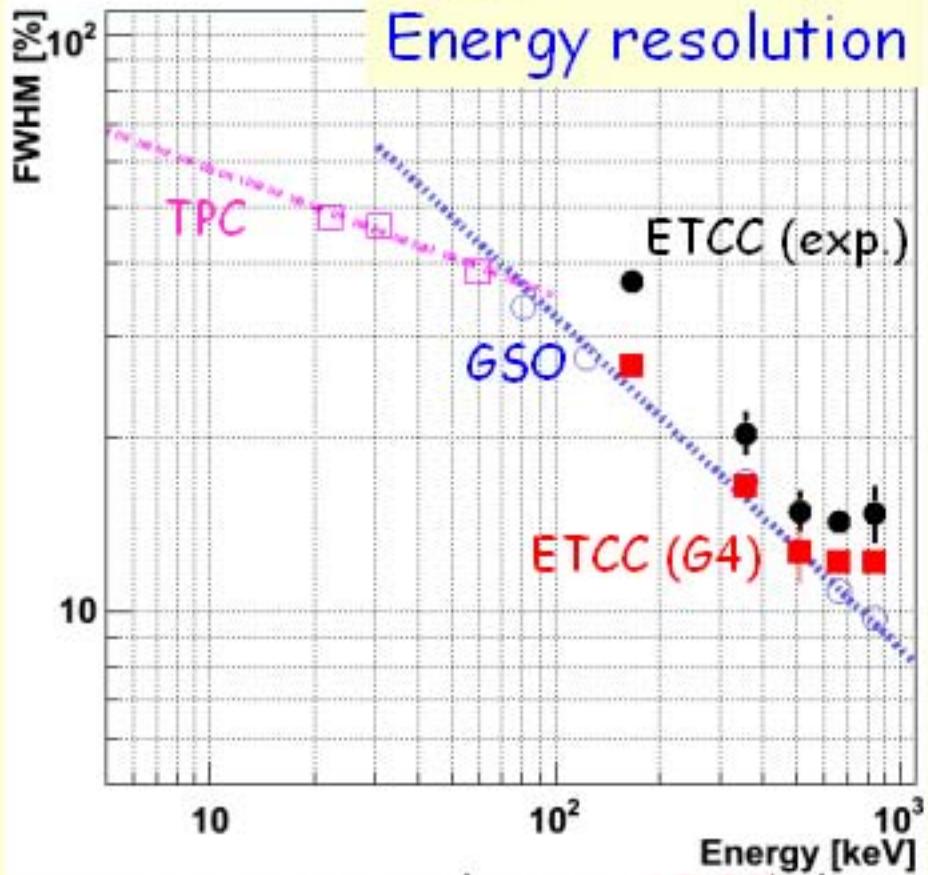
Black : Experiment  
Red : Geant4



Detection efficiency :  $\sim 2.5 \times 10^{-4}$

Field Of View :  $\sim 4$  steradian (FWHM)

# Energy/Angular Resolution



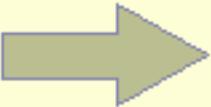
Energy resolution : 12.2% (Geant4) ⇔ 14.3% (experiment)  
@ 662keV FWHM

Angular resolution : ARM 10.9° (Geant4) ⇔ 8.9° (experiment)  
SPD 75.1° (Geant4) ⇔ 77.8° (experiment)  
@ 662keV HWHM

# Summary & Future Work

- We constructed the simulator for the Electron Tracking Compton Camera (ETCC).
- Absorber :  
Energy resolution, Distorted image  $\Rightarrow$  roughly consistent
- Tracker :  
Energy resolution, Tracking  $\Rightarrow$  roughly consistent
- ETCC :  
Detection Efficiency, Energy resolution, Angular resolution  
 $\Rightarrow$  roughly consistent with calibration

In more detail...

- ▶ Gas gain distribution for 1 electron
  - ▶ Update the response template of preamp
  - ▶ Electrical noise
  - ▶ etc... 
- Check the rejection power for p/n
  - Background simulation at balloon altitude
  - Study for the analysis
  - Design for the next balloon experiment